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Tamatakon01

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Definition 1 : Let \mathbb{N} denote the set of all natural numbers

Definition 2 : FOL is defined by adding a 1-ary function symbol f to the language of first order set theory with countably many variable term symbols and the set-membership relation symbol \in .

Definition 3 : For any formal language \mathcal{L} , let $\text{Shar}(\mathcal{L})$ denotes the power set of all "well-formed formulas + ACA_0 in \mathcal{L} " where $\text{ACA}_\mathcal{L}$ denotes ACA_0 written in \mathcal{L} .

Definition 4 : Δ_0 is the set that does not contain unbounded quantification.

Definition 4a : a theory is the set of sentences in any formal language

Definition 5 : Let Re denote the class of all recursive ordinal

Definition 6 : a binary relation \prec is called **QI** if it satisfies the following properties:

$$\begin{aligned} &(\forall x)[\neg x \prec x] \wedge \\ &(\forall x)(\forall y)[x \prec y \vee x = y \vee y \prec x] \wedge \\ &(\forall x)(\forall y)(\forall z)[x \prec y \wedge y \prec z \rightarrow x \prec z] \wedge \\ &(\forall X \subseteq \mathbb{N})[(\forall x)[(\forall y \prec x)[y \in X] \rightarrow x \in X] \rightarrow (\forall x)[x \in X]] \end{aligned}$$

Definition 7 : For any sufficiently strong theory T

$$\text{PTO}(T) := \sup\{\text{otyp}(\prec) \mid \prec \subseteq \mathbb{N}^2 \wedge \prec \in \Delta_0 \wedge T \vdash \prec \text{ is } \mathbf{QI}\}$$

Definition 8 : Let $\text{el} : \text{Shar}(\text{FOL}) \rightarrow \mathbb{N}, n \mapsto \text{el}(n)$ is a gödel number function, 1 - 155063 is all unicode version 16.0 characters ordered using unicode convention and after that it followed by infinitely many constant symbol, infinitely many variable symbol, n -ary predicate symbol, and n ary relation symbol, using veritasium hilbret hotel video scheme, thou shall know that!

Definition 8a : for any set S binary relation \in_{sub} defined by the following:

$$\forall p(p \in_{\text{sub}} S \leftrightarrow \exists k(k \subseteq S \wedge p \in k))$$

Definition 8b : for any $a \in \text{Shar}(\text{FOL})$, for any $b \in \text{Shar}(\text{FOL})$ binary relation $<_{\text{el}}$ be defined by the following :

$$a <_{el} b \leftrightarrow \text{el}(a) < \text{el}(b)$$

Definition 9 : Let a set

$$S = (\{T \in_{sub} \text{Shar}(\text{FOL}) | \text{PTO}(T) < \omega_1^{CK}\}, \in_{el})$$

Definition 10 : Let a function $h : \mathbb{N} \rightarrow \mathcal{P}(S), n \mapsto h(n)$ as

$$\{T \in_{sub} \text{Shar}(\text{FOL}) | h(T) < n, \forall n \in \mathbb{N}\}$$

Definition 10a : Let STM denote the set of all turing machine

Definition 10b : $\text{ProvableTermination}(T_q, M, p)$ holds if and only if there exists a formal proof in the theory T_q (using at most p symbols) of the statement "Turing machine M halts on all inputs"

Definition 10c: $\text{Halts}(M, N)$ holds if and only if Turing machine M halts (on the empty input) within N computation steps.

Definition 11: for every natural number p and q , let a function $g : \mathbb{N} \times \mathbb{N} \rightarrow \mathbb{N}$ as

Let a natural number

$$Q = \min \left\{ N \in \mathbb{N} \mid \begin{array}{l} \forall M \in \text{STM}, \forall T_q \in S(p), \\ (\text{ProvableTermination}(T_q, M, p) \implies \text{Halts}(M, N)) \end{array} \right\}$$

If $Q \in \mathbb{N}$: $g(p, q) = Q$ otherwise $g(p, q) = 1$

Definition 12: a function $k : \mathbb{N} \rightarrow \mathbb{N}, n \mapsto k(n)$ as

$$k(n) = \sum_{k=0}^n g(n, k)$$

Final: Coin a number Shèhuì zhǔyì guójiā rénmin dìwèi gāo bǎn yī as $k^i(i)$ where i is meta natural number $12 \uparrow^{12} 12$ with respect to uparrow notation